Principles of Programming Languages Small examination

Student ID:

Name:

Problem 1 Illustrate the quilts represented by the following expressions (1), (2), and (3) in the language Little Quilt.

The meaning of a, b, turn, sew are as follows. The other constructs of Little Quilt (let expressions, val declaration, fun declaration) have the meaning explained in the lecture.

• Expressions a and b represent the quilts in Figure 1 and Figure 2 respectively.





Figure 1: The quilt that a represents Figure 2: The quilt that b represents

- The expression turn (e) represents the quilt obtained by rotating 90 degrees to the right the quilt represented by the expression e.
- The expression sew (e_1, e_2) represents the quilt that is obtained by sewing the two quilts e_1 and e_2 , where e_1 is in the left side and e_2 is in the right side, and they must have the same height.

Problem 2 Answer the following problems about the control flow in the imperative language presented in the lecture.

(1) Illustrate the control flow of the following program fragment.

```
if x>0 then x := x - 1
else if y>0 then y := y - 1
else y := y + 1
```

(2) Illustrate the control flow of the following program fragment.

```
x := 10;
sum := 0;
L: sum := sum + x;
x := x - 1;
if x>0 then
    goto L
```

(3) Illustrate the control flow of the following program fragment.

```
while x>0 do
   begin
        if x=3 then
        begin
            x := x - 1;
            continue
        end;
        y := y + 1;
        x := x - 1
   end
```

(4) Illustrate the control flow of the following program fragment.

```
while x>0 do
    begin
    while y>0 do
        begin
        if x=3 then
        break;
        z := z + 1;
        y := y - 1
        end;
        x := x - 1
    end
```

(5) How many entries and exits does the if statement (if x=3 then break;) in the program fragment (4) have?

Problem 3 Derive the Hoare triples (1), (2), and (3) by using the rules presented in the lecture.

(1)
$${a = 3} \ a := a + 1 \ {a = 4}$$

(2)
$${a = 3} \ a := a + 1; a := a + 2 {a = 6}$$

(3)
$$\{a=4\}$$
 if $a=4$ then $a:=a+2$ else $a:=a-3$ $\{a=6\}$

(4)
$$\{a=5\}$$
 while $a>0$ do $a:=a-1$ $\{a=0\}$

Problem 4

Show the output produced by executing the following Pascal program. When the keyword var is attached to a formal parameter, it designates the parameter as call-by-reference. The procedure writeln writes out to the standard output the value of the parameter and a new line character.

```
program test;
                                    begin
var x : integer;
                                       x := 3;
var y : integer;
                                       y := 4;
procedure swap
                                       swap (x,y);
  (var x: integer;
                                       writeln (x);
   var y : integer);
                                       writeln (y)
var z : integer;
                                    end.
begin
   z := x; x := y; y := z
end;
```

Problem 5

Show the output produced by executing the following Pascal program. Note that Pascal is statically (lexically) scoped.

Rules presented in the lecture

Hoare logic

$$\frac{\{P\}\ S_1\ \{Q\}\ \{Q\}\ S_2\ \{R\}}{\{P\}\ S_1;\ S_2\ \{R\}} \text{ (composition rule)}$$

$$\frac{\{P\ \land\ E\}\ S_1\ \{Q\}\ \{P\ \land\ \neg\ E\}\ S_2\ \{Q\}}{\{P\}\ \text{if } E \text{ then } S_1 \text{ else } S_2\ \{Q\}} \text{ (conditional rule)}$$

$$\frac{\{P\ \land\ E\}\ S\ \{P\}}{\{P\}\ \text{while } E \text{ do } S\ \{P\ \land\ \neg\ E\}} \text{ (while rule)}$$

$$\frac{\{Q[E/x]\}\ x\ :=\ E\ \{Q\}}{\{P\}\ S\ \{Q'\}\ Q'\Rightarrow Q} \text{ (consequence rule)}$$