

Principles of Programming Languages

Answers for small examination 2

Problem 1 Show the type consistency of the following program fragment, which is written in the subset of C language presented in the lecture, according to (1) and (2).

(Answer)

```
int *p;
int x[3];
p = x;
```

- (1) Rewrite the variable declarations `int *p;` and `int x[3];` in the postfix notation presented in the lecture.

(Answer)

```
p : int *
x : int [3]
```

- (2) Show the type consistency of the assignment expression `p=x` by applying the inference rules to the declarations of `p` and `x` in the postfix notation obtained in (1).

(Answer)

$$\frac{\begin{array}{c} x : \text{int } [3] \\ p : \text{int } * \quad x : \text{int } \& \end{array}}{p = x : \text{int } \&}$$

Problem 2 A lambda expression $(\lambda x. \lambda y. x) ((\lambda z. z) w)$ can be transformed to $(\lambda y. w)$ by applying the β reductions. Write the each step of the β reductions. (Although there are more than one sequences of β reductions, write one of them.)

(Answer 1)

$$(\lambda x. \lambda y. x) ((\lambda z. z) w) \xrightarrow{\beta} (\lambda x. \lambda y. x) w \xrightarrow{\beta} \lambda y. w$$

(Answer 2)

$$(\lambda x. \lambda y. x) ((\lambda z. z) w) \xrightarrow{\beta} \lambda y. ((\lambda z. z) w) \xrightarrow{\beta} \lambda y. w$$

Problem 3 Write the output to the display when executing the following program in C++.

```
#include <stdio.h>
class B {
public:
    virtual char f() { return 'B';}
    char g() { return 'B'; }
```

```

    char testF(B *b) { return b->f();}
    char testG(B *b) { return b->g();}
};
class D : public B {
public:
    char f() { return 'D';}
    char g() { return 'D';}
};
int main(void) {
    D *d = new D;
    printf("%c%c\n", d->testF(d), d->testG(d));
    return 0;
}

```

(Answer)

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Problem 4

Show the meaning of the following programs (1) and (2) by using the rules presented in the lecture. Note that the programs are in the small subset of C presented in the lecture. Let the states before executing the programs both to be $\sigma = \{(X, 3), (Y, 1), (Z, 0)\}$.

(1) `Z=(X+4);`

$$\frac{\frac{\langle X, \sigma \rangle \rightarrow 3 \quad \langle 4, \sigma \rangle \rightarrow 4}{\langle (X + 4), \sigma \rangle \rightarrow 7}}{\langle Z = (X + 4);, \sigma \rangle \rightarrow \sigma[7/Z]}$$

So in the state σ , after executing the program `Z=(X+4);` the state becomes as follows.

$$\sigma[7/Z] = \{(X, 3), (Y, 1), (Z, 7)\}$$

(2) `while(Y){Y=(Y-1);}`

$$\frac{\frac{\frac{\langle Y, \sigma \rangle \rightarrow 1 \quad \langle 1, \sigma \rangle \rightarrow 1}{\langle (Y - 1), \sigma \rangle \rightarrow 0}}{\langle Y, \sigma \rangle \rightarrow 1 \quad \langle Y = (Y - 1);, \sigma \rangle \rightarrow \sigma[0/Y]} \quad \frac{\langle Y, \sigma[0/Y] \rangle \rightarrow 0}{\langle \text{while}(Y)\{Y = (Y - 1);\}, \sigma[0/Y] \rangle \rightarrow \sigma[0/Y]}}{\langle \text{while}(Y)\{Y = (Y - 1);\}, \sigma \rangle \rightarrow \sigma[0/Y]}$$

So in the state σ , after executing the program `while(Y){Y=(Y-1);}` the state becomes as follows.

$$\sigma[0/Y] = \{(X, 3), (Y, 0), (Z, 0)\}$$